## **Statistics Canada International Symposium Series - Proceedings**

### Symposium 2006 : Methodological Issues in Measuring Population Health



2006



Statistics Canada

Statistique Canada



# Estimating Sample Size for Complex Surveys: Building Consensus in an Environment of Multiple Hypotheses, Multiple Stakeholders and Limited Budgets

Victor JC, O'Connor S, Diemert LM, Bondy S, Brown KS, Cohen J, Ferrence R, Garcia J, McDonald P, Selby P, Stephens T<sup>1</sup>

#### **Abstract**

How does one efficiently estimate sample size while building concensus among multiple investigators for multi-purpose projects? We present a template using common spreadsheet software to provide estimates of power, precision, and financial costs under varying sampling scenarios, as used in development of the Ontario Tobacco Survey. In addition to cost estimates, complex sample size formulae were nested within a spreadsheet to determine power and precision, incorporating user-defined design effects and loss-to-followup. Common spreadsheet software can be used in conjunction with complex formulae to enhance knowledge exchange between the methodologists and stakeholders; in effect demystifying the 'sample size black box'.

KEY WORDS: Sample size, Population-based Survey, Study Design.

#### 1. Introduction

Few researchers would disagree that adequate sample size is critical to good study design. Sample size calculations for experimental and observational studies are often easily performed through use of standard formulae and sample size software. However, deriving appropriate sample size estimates for a study is complicated when the study is examining multiple outcomes and/or multiple exposures. The utility of standard formulae and software is limited when determining sample size for broad surveys of the general population. These surveys may be designed for multiple purposes such as developing population estimates of both outcomes and exposures, and testing hypotheses. Often, these surveys also involve multiple investigators, with different research foci.

We present the approach taken by the Ontario Tobacco Research Unit (OTRU) to develop the design and sample size required for its Ontario Tobacco Survey (OTS). The OTS is a regionally-stratified telephone survey of over 7500 adult smokers and non-smokers residing in Ontario. The survey incorporates a rolling longitudinal component that surveys smokers, and a cross-sectional component surveying non-smokers. We describe this approach as a potential guide for other research groups undertaking the development of a large-scale, multipurpose survey.

#### 2. Background

The Ontario Tobacco Research Unit is an academic unit with offices at the Centre for Addiction and Mental Health, the University of Toronto and the University of Waterloo in Ontario, Canada. The research direction of the unit is managed by a team of seven principal investigators.

<sup>&</sup>lt;sup>1</sup>J. Charles Victor, Shawn O'Connor, Lori M. Diemert, Susan Bondy, K. Stephen Brown, Joanna Cohen, Roberta Ferrence, John Garcia, Paul McDonald, Peter Selby, Thomas Stephens, Ontario Tobacco Research Unit, 33 Russell St. Toronto, Ontario, Canada M5S 2S1. Corresponding author's email: charles victor@camh.net.

The Ontario Tobacco Research Unit is tasked with providing timely research on the status of tobacco use in the province of Ontario. In addition to providing annual estimates of tobacco-related outcomes and exposures, OTRU also evaluates the policies and initiatives of the Government of Ontario to stem tobacco use in the province. To accomplish these goals, OTRU has, for years, used provincial surveys (e.g., Centre for Addiction and Mental Health Monitor (CAMH Monitor) and Ontario Student Drug Use Survey) and national health surveys (e.g., Canadian Community Health Survey and Canadian Tobacco Use Monitoring Survey). However, these surveys often did not fully meet OTRU's needs. The Ontario based surveys are focussed on a range of mental health issues and addictions, providing only moderate content for tobacco-related questions. National surveys either provided small sample sizes for Ontario, or did not provide adequate tobacco-related content. As the prevalence of smoking declines in Ontario (Ontario Tobacco Survey Research Unit, 2006) the data from these surveys are increasingly insufficient to perform sub-group analysis. As a result, OTRU committed to developing an Ontario-based population survey that would both provide periodic estimates of tobacco-related outcomes and exposures, and enable longitudinal hypothesis testing with adequately large sample sizes to allow small sub-group analyses.

#### 3. Planning the Design and Determining Sample Size

The first step in the development of the OTS was to determine the design. Several options were considered including fully cross-sectional, fully longitudinal, and a combined longitudinal/cross-sectional hybrid. Given the multiple goals of the survey and the different research foci of the seven principal investigators of the research unit, it was decided to combine a longitudinal component with a cross-sectional component. However, the precise nature of the two components, and stratification of the sampling frame remained difficult to define. The barriers to moving forward with the design of the survey included determining the power to evaluate multiple hypotheses while remaining within our budget allocation. Several sample size calculations proved unfruitful in the design process, as these calculations were static, and did not address the questions of all investigators.

#### 3.1 Development of a Design and Sample Size Tool

Due to the complex longitudinal/cross-sectional hybrid design, we began work on a spreadsheet to estimate costs for given designs and numbers of participants (Figure 1: all figures at end of text).

This first screen of the tool allowed the user to input the number of smokers sampled into a longitudinal component and additionally into a cross-sectional component (if required), as well as the number of non-smokers sampled into a cross-sectional component. The tool was designed to account for user-defined loss-to-follow-up rates, and whether losses would be replaced in subsequent waves. Finally, the 'Design' page allowed the user to enter the estimated cost per interview, and thus the cost over the study period.

One goal of the survey was to determine statistically stable population estimates of tobacco-related outcomes and exposures in specific age groups and regions. A decision was made to sample within regions of Ontario, defined by telephone area codes, in order to achieve adequate sample in the northern regions of the province. Furthermore, the decision was made not to sample based on age, but to choose a sample size that would provide sufficient numbers of participants between the ages of 18 and 30 years. To estimate the number of participants in each smoking status by age by region subgroup, a second page was added to the design tool that estimated the allocation of the sample size in each of these strata based on 2001 census information and smoking prevalence from the 2002 CAMH-M (Figure 2). While not visible in Figure 2, several stratification scenarios were evaluated on this page (e.g., combining 416 and 905 telephone exchanges vs. separating these exchanges). The estimates provided on the second page of the tool are linked with the user-defined inputs from the first page allowing real-time evaluation of different sample sizes and their impact on the age, regional, and smoking status make up of the final sample.

To evaluate the ability of the cross-sectional components of the survey to provide precise and stable population estimates of tobacco-related outcomes and exposures, a third page was added to the tool (Figure 3). Formulae to calculate the width of 95% confidence intervals for estimates of proportions of 5%, 25% and 50% were integrated into the page. Due to the complex nature of the sampling for the survey, traditional asymptotic confidence interval

formulae would provide biased and often smaller widths. Thus the formulae used were adjusted according to Lohr (1999) to account for the estimated design effects (DEFFs). An input field on the page allowed the user to enter the estimated DEFFs and view changes to the precision of estimates. Moderate values between 1.5 and 2.0 were used for estimating precision for the OTS survey (Lohr, 1999). This page stratified estimates by smoking status and age group, allowing users to see the precision of analyses for sub-groups of particular interest.

While the third page of the tool ("Precision), was integral in evaluating the ability of the survey to provide estimates, a fourth and fifth page were added to calculate power for research hypotheses. The fourth page calculated power for both user-defined and preset cross-sectional odds ratios incorporating the user-defined design effects linked from the previous page (Figure 4). The final page was used to calculate power for longitudinal analyses (two timepoints), for both binary and continuous outcomes (Figure 5); again, these formulae incorporated the user-defined DEFFs entered on the third page (Lohr, 1999; Rosner, 1995).

#### 4. Discussion

Developing a complex survey reporting multiple population estimates and testing multiple hypotheses while being cost-effective requires a multi-faceted approach to sample size estimation. However, the development of a sample size tool such as that developed for the OTS is not always warranted. Indeed commercial sample size calculators and/or good references for sample size forumlae (see Fleiss, 2003; Lohr, 1999; Rosner, 1995) may be all that investigators need during the initial planning phase of a project. However, these common tools fail for many reasons on more complex research studies such as general population surveys. First, these tools make it difficult to readily examine several hypotheses at the same time. Secondly, the interface often precludes simple real-time adjustments to parameters and revised results. That is, the sample size programs, and certainly statistical formulae are not easily accessed nor understood by all investigators. Often there needs to be a facilitator (the analyst), to guide the derivation and interpretation of results. Finally, there is frequently a disconnect between the investigators that are concerned about the budgetary constraints of the research project, and the analyst who is concerned with developing an accurate estimate of sample size required to achieve the greatest statistical power. By incorporating sample size and power formulae into common spreadsheet software along with design information and assumptions (e.g., loss-to-follow-up), and cost information, one is able to marry all of these aspects into one tool that is accessible to most investigators.

We found the most effective use of this tool was at team meetings where, equipped with a laptop computer and projector, the analyst was able to use the tool and alter the parameters of design and sample size according to multiple team members' questions. The provision of immediate responses expedited the design and sample size process. Possibly the most novel and important feature of the tool was the integration of the attrition and cost estimate function. These functions made it possible to immediately evaluate the financial feasibility of design suggestions and requested for sample sizes, while ensuring that adequate power was maintained. Following team meetings, the sample size tool was made available to all team members. Given its common spreadsheet platform, this made the tool usable by all investigators that wished to examine different design scenarios outside of the group meetings.

#### 5. Recommendations

For research teams considering large projects that may have multiple hypotheses or purposes, multiple investigators, and limited budgets we strongly suggest the development of a tool similar to that which is presented here. We advise the development of a common spreadsheet tool where the analyst incorporates:

- 1) The possible designs of the study
- 2) User-defined estimates of attrition and cost
- 3) Published sample size formulae (include design effects where appropriate)

We advise the use of this tool in team meetings, where the real-time capabilities of this tool can have the greatest impact. This particular tool is not designed to calculate sample size calculations for highly complex analyses (e.g. multi-level modelling). The greatest utility to these tools is most likely for broad surveys of the general population. Nonetheless, many complex sample size formulae could easily be incorporated into a tool such as this with the proper expertise.

#### References

Fleiss, JL., Levin B., Paik MC. (2003), Statistical Methods for Rates and Proportions 3<sup>rd</sup> ed., New York: Wiley.

Lohr S. (1999), Sampling: Design and Analysis, Pacific Grove CA: Duxbury Press.

Ontario Tobacco Research Unit (2006). *Indicators of Smoke-Free Ontario Progress*. [Special Reports: Monitoring and Evaluation Series, 2005-2006 (Vol. 12, No. 2)]. Toronto, ON: Ontario Tobacco Research Unit.

Rosner B. (1995), Fundamentals of Biostatistics, Boston: Duxbury.

Figure 1: Design and Cost Calculations of Spreadsheet Tool to Develop Sample Size for Complex Projects

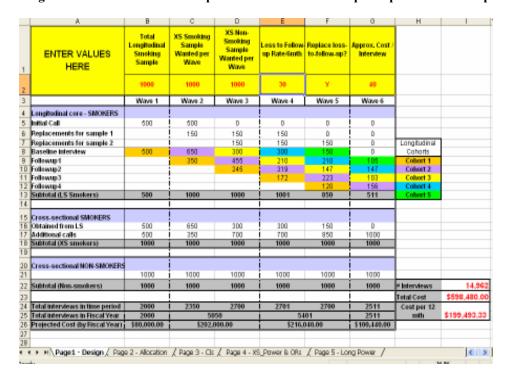


Figure 2: Allocation of Sample Size Across Statification Scenarios

	А	В	С	D	E	F	G	Н	T I	J
1	Using 5 Area	Code Regions								
2	1999	REGION		807/705				613	ji	
3				Age				Age		
4	Smoking Stat	us	18-29	30+	Total		18-29	30+	Total	
5	Smoker	Daily	84	91	175		84	89	173	
6		Occasional	16	9	25		16	11	27	
7	Non-Smoker	Former	11	45	56		10	37	47	
8		Never	89	55	144		90	63	153	
9	Total		200	200	400		200	200	400	
10						111				
11		REGION		416/647				905/289		
12				Age				Age		
13	Smoking Stat	us	18-29	30+	Total		18-29	30+	Total	
14	Smoker	Daily	73	85	158	- 1	79	88	167	
15		Occasional	27	15	42		21	12	33	
16	Non-Smoker	Former	11	25	36		9	33	42	
17		Never	89	75	164		91	67	158	
18	Total		200	200	400	T. I	200	200	400	
19										
20		REGION		519			ALI	L REGIONS	S	
21				Age				Age	19	
22	Smoking Stat	us	18-29	30+	Total		18-29	30+	Total	
23	Smoker	Daily	84	90	174	Ť	404	443	847	
24		Occasional	16	10	26		96	57	153	
25	Non-Smoker	Former	10	39	49		51	179	230	
26		Never	90	61	151		449	321	770	
27	Total		200	200	400		1000	1000	2000	
28	*Occasional Smok	ers Defined using OT	RU definition of	those smoki	na > 1 and <	30 ciga	rettes in the pa	st 30 days +	> 100 cigarette	es in
29		Region Specific alloca								
30		1   522   11			- C - C - C - C - C - C - C - C - C - C					
31										
	A NA Droot	- Design \ Page 2	Allocation	a / Daga 2	CIc / Do	221		- 10	- 1	

Figure 3. Precision Estimates (95% Confidence Interval Widths) Based on Sample Size, Allocation and Design Effects

	Α	B C	D	E	F	G	Н	I	J	
1	Enter	DEFF		Precision	for perce	ntages. W	/idth of 95	% confider	ice bands	
2	2	2.0		1100000	ioi perce		percent	, cominaci	ice ballas	
3					Ex	pected Val	ues			
4					5%	25%	50%			
5	Provincia	l Estimates			±	±	±			
6	Smoker		1000		1.9	3.8	4.4			
7		Daily Smoker	847		2.1	4.1	4.8			
8		Occasional Smoker	153		4.9	9.7	11.2			
9										
10	Non-Smo	ker	1000		1.9	3.8	4.4			
11		Former	230		4.0	7.9	9.1			
12		Never	770		2.2	4.3	5.0			
13										
14	Analyses	Restricted to <30 yrs	old		±	±	±			
15	Smoker		500		2.7	5.4	6.2			
16		Daily Smoker	404		3.0	6.0	6.9			
17		Occasional Smoker	96		6.2	12.3	14.1			
18										
19	Non-Smo	ker	500		2.7	5.4	6.2			
20		Former	51		8.5	16.8	19.4			
21		Never	449		2.9	5.7	6.5			
22										
23	Analyses	Restricted to 30+ yrs	old		±	±	±			
24	Smoker		500		2.7	5.4	6.2			
25		Daily Smoker	443		2.9	5.7	6.6			
26		Occasional Smoker	57		8.0	15.9	18.4			
27										
28	Non-Smo	ker	500		2.7	5.4	6.2			
29		Former	179		4.5	9.0	10.4			
30		Never	321		3.4	6.7	7.7			
31		age1 - Design / Page								

Figure 4: Power Calculation for Cross-sectional Study Odds Ratios Based on Sample Size, Allocation, and Design Effects

	A	В	С	D	E	F	G	Н		J	K	
1	Pov	ver Calc	ulatio	ns for s	imple OR	's	from	XS st	udy			
3	Ente	r		В	ecall:							_
4	Proportion of 'unexposed' having factor of interest in %	Odds Ratio	p(ezp) %	XS Smokers	1000		(N=1000 S	s of Minim mokers and Smokers)*	d 1000 Non-			
5	5.0	2	9.5	XS NonSmoker	1000		Expect	ed Outcom	e Rates			
6	Provincial Estima	tes"		n	Power	Ĭ	5%	10%	25%			
7	Smoker			1000	78		2.02	1.71	1.48			
8		Daily Smoke		847	71		2.14	1.78	1.53			
9		Occasional	Smoker	153	19		>4.00	3.43	2.62			
10												
	Non-Smoker			1000	78		2.02	1.71	1.48			
12		Former		230	26		3.70	2.80	2.20			
13		Never		770	67		2.20	1.83	1.56			_
14						_						-
	ENTIRE SAMPLE			2000	97		1.68	1.48	1.32			-
16					_						-	-
	Analyses Restrict	ed to <30 grs	old-	n	Power				470		-	+
	Smoker			500	49	_	2.60	2.08	1.73		-	+
19		Daily Smoke		404	41	_	2.82		1.83		-	+
20		Occasional	omoker	96	13		>4.00	>4.00	3.30		-	+
	Non-Smoker			500	49	_	2.60	2.08	1,73		-	+
23	Non-Smoker	Former		51	9	_	>4.00	>4.00	>4.00		-	+
24		Never		449	45		2.70	2.15	1,78		-	+
25		Ideaei		773	70		2.70	2.10	1.70		-	+
	ENTIRE SAMPLE			1000	78		2.02	1.71	1.48			_
27												_
28	Analyses Restrict	ed to 30+ urs	old"	n	Power	1						-
	Smoker			500	49		2.6	2.08	1.73			
30		Daily Smoke	r	443	45		2.72	2.16	1.79			
31		Occasional S		57	10		>4.00	>4.00	>4.00			
32												
33	Non-Smoker			500	49		2.60	2.08	1.73			
34		Former		179	21		>4.00	3.18	2.50			
35		Never		321	34		3.15	2.43	1.96			
36												
	ENTIRE SAMPLE			1000	78		2.02	1.71	1.48			
38	* All analyses are two-tail							es are two-t	ailed, with alpl	ha=0.05 beta:	:0.80	
14 4	L ▶ MIZ Page 3.	- CIs \ Page	e 4 - XS	Power & I	DRs / Page 5	- L c	<					>
	, , , , , , , , , , , , , , , , , , ,						-					-

Figure 5. Power Calculation for Longitudinal Differences in Binary and Continuous Outcomes Based on Sample Size, Allocation, and Design Effects

_	A						
3	Analyses of	Proportions		-	Analyses of	Mean Ch	ange
4	Proportion maintaining some factor b/w timepoints:	Odds Ratio of Favourable Direction of Change					
5	respond yes or no to quit attempt at	(ie Odds of quitting smoking b/w T1.T2 compared to odds of taking up smoking among former smokess)		Mean ()	lifference	Variance	of Difference
-							
1	85	2			7		139
	<b>8</b> 5	2			7 Danier to de	to et a diffe	
	85 Provincial Estimates	. 2	,	Powe	Power to de r for OR		
			1000				rence
0 5	Provincial Estimates	Daily Smokers			r for OR		rence Mean Difference
0 5	Provincial Estimates		1000		r for OR 92		rence Mean Difference
0 5	Provincial Estimates	Daily Smokers Occasional Smokers	1000 820		r for OR 92 91		rence Mean Difference 100 100
0 9	Previncial Estimates Smokes	Daily Smokers Occasional Smokers	1000 820 180		r for OR 92 91		rence Mean Difference 100 100
0 5	Provincial Estimates Smokers Analyses Restricted I	Daily Smokers Occasional Smokers	1000 820 180		r for OR 92 91 81		Mean Difference 100 100 100
7 9 9 1 0 1 2 3 4 4 7	Provincial Estimates Smokers Analyses Restricted I	Daily Smokers Occasional Smokers to <30 yes old*	1000 820 180 1		r for OR 92 91 81		Neam Difference 100 100 100
7 8 9 1 1 2 3 4 4 4 6 6 7 8	Provincial Estimates' Smokers Analyses Restricted t Smoker	Daily Smokers Occasional Smokers to <30 yes old* Daily Smoker Occasional Smoker	1000 820 180 180 800 410		r fee OR 92 91 91 81		Mean Difference 100 100 100 100 100
0 1 1 2 3 4 4 7 8	Provincial Estimates' Smokers Analyses Restricted t Smoker Analyses Restricted t	Daily Smokers Occasional Smokers to <30 yes old* Daily Smoker Occasional Smoker	1000 820 180 180 800 410		r fee OR 92 91 91 81 87 86 77		Mean Difference 100 100 100 100 100
7 3 9 9 1 2 3 4 4 7 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	Provincial Estimates' Smokers Analyses Restricted t Smoker	Daily Smokers Occasional Smokers to <30 yes old* Daily Smoker Occasional Smoker	1000 820 180 180 500 410 90		r fee OR 92 91 91 81		Mean Difference 100 100 100 100 100
10 9 11 12 13 14 4 15 9 16 17	Provincial Estimates' Smokers Analyses Restricted t Smoker Analyses Restricted t	Daily Smokers Occasional Smokers to <30 yes old* Daily Smoker Occasional Smoker	1000 820 180 180 500 410 90		r fee OR 92 91 91 81 87 86 77		Mean Difference 100 100 100 100 100 100 98